Admission Control for Statistical QoS: Theory and Practice^{*}

Edward W. Knightly[†] Rice University knightly@ece.rice.edu Ness B. Shroff[‡] Purdue University shroff@ecn.purdue.edu

Abstract

In networks that support Quality of Service (QoS), an admission control algorithm determines whether or not a new traffic flow can be admitted to the network such that all users will receive their required performance. Such an algorithm is a key component of future multi-service networks as it determines the extent to which network resources are utilized and whether the promised QoS parameters are actually delivered. Our goals in this paper are threefold. First, we describe and classify a broad set of proposed admission control algorithms. Second, we evaluate the *accuracy* of these algorithms via experiments using both on-off sources and long traces of compressed video; we compare the admissible regions and QoS parameters predicted by our implementations of the algorithms with those obtained from trace-driven simulations. Finally, we identify the key aspects of an admission control algorithm necessary for achieving a high degree of accuracy and hence a high statistical multiplexing gain.

1 Introduction

Provisioning network resources to meet the Quality of Service (QoS) demands of bursty traffic sources is a key issue for future multi-service networks. Such resource provisioning may be realized by an admission control algorithm, which has the function of limiting the number of traffic flows in a class such that the required QoS constraints can be satisfied. The design of admission control algorithms has important consequences for network performance, as an algorithm that unnecessarily denies access to flows that could have been successfully admitted will under-utilize network resources; similarly, an algorithm that incorrectly admits too many flows will induce QoS violations.

Unlike a deterministic service [2], a statistical or soft real-time service associates a small *violation* probability with delay and throughput bounds, as needed to obtain a utilization gain over a purely worst case approach. Developing resource allocation schemes for a statistical service has proven particularly challenging due to both the multiple-time-scale characteristics of many multimedia applications, e.g., [3, 4, 5], as well as potential intractabilities arising from complex interactions among traffic flows and the shared multiplexer.

Our goals in this paper are threefold. First, we describe a broad set of admission control algorithms from the literature which we divide into the following five classes: (1) tests based on average and peak rate combinatorics [6, 7], (2) tests based on additive effective bandwidths [8, 9, 10, 11], (3) tests based on engineering the "loss curve" [12, 13, 14, 15], (4) tests based on maximum variance approaches [16, 17, 18], and (5) tests based on refinements of effective bandwidths using large deviations theory.

Second, we perform a large number of experiments to evaluate the accuracy and effectiveness of these admission control algorithms under realistic workloads, namely, thirty-minute traces of variable-rate MPEG-compressed video and exponential on-off sources commonly used to model voice traffic. To achieve this, we first implement a number of algorithms from the aforementioned classes and determine their respective admissible regions for various traffic mixes and QoS parameters. We then simulate a 45 Mbps multiplexer servicing the same traffic mix, with each flow's arrival sequence given by either a video trace with a random start time, or an on-off source. For each combination of traffic flows and a particular buffer size, we measure the flows' resulting performance parameters. By comparing the measured admissible regions with those

^{*}Excerpts of this paper appear in [1].

[†]The research of E. Knightly is supported by NSF CAREER Award ANI-9733610, NSF Grant ANI-9730104, Nokia Corporation, the Texas Advanced Technology Program, and Texas Instruments.

[‡]The research of N. Shroff is supported by the NSF CAREER Award NCR-9624525, and NSF Grants ANI-9805441, CDA-9422250, and CDA 96-17388.

predicted by the algorithms, we assess an algorithm's *accuracy*, i.e., its effectiveness in predicting QoS parameters and controlling the admissible region.

Finally, from our experimental results, we identify the components of an admission control test essential to achieving a high degree of accuracy and find that (1) the assumption of a bufferless multiplexer has a significant utilization penalty, (2) an algorithm must exhibit economies of scale in the number of multiplexed flows, (3) observed shapes of the "loss curve" can be quite different than the commonly assumed exponential relationship, (4) the traffic model, or parameters used to describe the properties of traffic flows to the network, requires more information than is currently standardized, and (5) an algorithm's accuracy with exponential on-off sources does not assure accuracy with bursty compressed-video sources.

In addition to the above classes of admission control algorithms, several other approaches have been developed, including measurement-based algorithms which control the admissible region based on aggregate traffic measurements [19, 20, 21, 22], enforceable statistical services which provision resources based on worst-case statistics of policed traffic flows [23, 24, 25] and algorithms for special-purpose systems such as video on demand [26, 27]. While review of such schemes is beyond the scope of this paper, we note that many of these approaches build on the theories and techniques which we *do* consider, so that our conclusions may provide guidelines for evaluating these schemes as well.

The remainder of this paper is organized as follows. First, in Section 2, we overview five classes of admission control algorithms. Next, in Section 3, we describe experimental results obtained from trace-driven simulations and our implementations of the admission control algorithms. Finally, in Section 4, we discuss the aspects of an algorithm most critical for achieving a high degree of accuracy, and in Section 5, we conclude.

2 Admission Control Tests for Statistical Service

In this section, we describe five classes of admission control tests that have been proposed for providing statistical QoS guarantees in multi-service networks. While these classes do not encompass all proposed schemes, they do provide broad coverage of the techniques applied to admission control. For QoS metrics, we consider two variations of what is commonly referred to as "loss probability". First, we denote the "tail probability" of the queue length distribution by P(Q > B), which refers to the fraction of time an infinite-buffer queue's occupancy exceeds B. Second, we denote the "loss probability" by P_l , which refers to the fraction of bits dropped by a queue that has finite buffer space B.

Throughout, we denote the link capacity by C and the buffer size by B, and denote the arrivals of traffic flow j in the interval [s, t] by $A_j[s, t]$.

2.1 Average/Peak Rate Combinatorics

In [7], source j is characterized by its peak rate $r_{pk,j}$ and average rate $r_{av,j}$. Assuming an on-off source that either transmits at its peak rate or is idle, the probability that the source is on is given by $p_{on,j} = r_{av,j}/r_{pk,j}$ and its rate distribution is given by

$$f_{j}(x) = \begin{cases} 1 - p_{on,j} & x = 0\\ p_{on,j} & x = r_{pk,j}\\ 0 & \text{otherwise.} \end{cases}$$
(1)

Using this rate distribution, an admission control algorithm is designed that approximates the packet loss probability for a bufferless multiplexer: in a bufferless multiplexer, packet loss occurs whenever the aggregate input arrival rate exceeds the link capacity. Since the distribution of the aggregate arrival rate of the multiplexed sources is given by a convolution of the individual $f_j(x)$'s, Lee et al. focus on efficient computation of the aggregate arrival rate distribution and subsequently the loss probability [7].

In [6], traffic flow j is also characterized by its peak and average rate. In contrast to [7] in which $r_{av,j}$ represents the long-term average rate, in [6] it refers to the worst-case rate over any interval of length I_j . That is, source j is constrained to send no more than $r_{av,j} \cdot I_j$ packets during any interval of length I_j (changing [6]'s notation for consistency). For Earliest Deadline First schedulers, Ferrari shows how to compute the probability of delay-bound violation by examining combinations of active flows (flows which are *on* with probability $p_{on,j}$) that may cause a delay-bound violation, and by summing their respective probabilities.

In this paper, we evaluate the test of [7], which we refer to as the "Avg/Peak" test.

2.2 Additive Effective Bandwidths

Various *effective bandwidth* admission control tests have been proposed in the literature including [8, 9, 10, 11]. In such schemes, each flow independently reserves a particular bandwidth between its average and peak rate. This bandwidth, termed *effective bandwidth*, is a function of the required loss probability P_l and the particular flow's stochastic properties (such as autocorrelation function, or peak and average rate together with mean burst duration). Once the effective bandwidth of flow j is determined, which we denote by $E_j(P_l)$ (or equivalently $E_j(P(Q > B))$), the admission control test requires that

$$\sum_{j=1}^{N} E_j(P_l) < C,\tag{2}$$

where N is the number of multiplexed flows. Effective-bandwidth type results have been devised using several inter-related techniques, including eigenvalue decomposition of Markovian flows [9], large deviations theory [8, 11], and the theory of envelope processes [28].

For example, [29] shows how the buffer occupancy distribution for Markov modulated fluid sources can be decomposed according to the eigenvalues of the aggregate Markovian arrival process. Since the overall tail probability P(Q > B) or loss probability P_l may be expressed as a sum of exponential terms, the largest eigenvalue, which we denote by δ , dominates with asymptotically large buffers. In other words, it has been found that the loss probability or (tail probability) satisfies the following relationship for some constant K

$$P_l \sim K e^{-\delta B},$$
(3)

where the similarity relationship $f(x) \sim g(x)$ of two functions $f(\cdot)$ and $g(\cdot)$ indicates that $\lim_{x\to\infty} f(x)/g(x) = 1$. In the additive effective bandwidth literature, the preterm K is approximated by¹ 1, or $P_l \approx e^{-\delta B}$. The admission control test amounts to ensuring that δ (the dominant eigenvalue) is large enough to meet the required loss probability constraint. For example, for on-off sources, the effective bandwidth can be computed using Equation (2) of [10].

Here, we evaluate the effective bandwidth test of [8] which has

$$E_j(P_l) = r_{av,j} + \frac{\delta \gamma_j}{2B} \tag{4}$$

where

$$\gamma_j = \lim_{t \to \infty} \frac{1}{t} \operatorname{var}(A_j[0, t])$$
(5)

is the arrival sequence's index of dispersion and $\delta = -\frac{\log(P_l)}{R}$.

Note that the effective bandwidth of a flow is independent of the properties of all other traffic flows as well as the number of sources N and the link capacity C: it is determined only by the stochastic properties of the flow itself, the required loss probability P_l , and the buffer size B.

2.3 Engineering the "Loss Curve"

We refer to a *loss curve* as the relationship between loss probability and buffer size, which, for additive effective bandwidths is exponential and given by $P_l \approx e^{-\delta B}$. As the $e^{-\delta B}$ approximation can be conservative for reasons outlined below, several techniques have been proposed which seek to engineer the shape of the loss curve to better reflect experimentally observed relationships.

The approach in [15] stems from a simple observation based on the authors' work in video modeling [30, 31, 32]. When the input traffic is highly correlated as in the case of JPEG-encoded video, a quasi-stationary approximation, called the histogram model [32] (or generalized histogram model [31, 33]) was found to be quite accurate because P_l does not significantly decrease when B is increased beyond a certain range (referred to as the *cell region*). However, when applying the histogram model to other less correlated sources, it was found that the model could not predict the loss behavior well for large buffer sizes. To overcome this difficulty, in [15], the authors use the histogram model for the cell region (small buffers), and a single exponential approximation for the burst region (large buffers), with the cutoff point found by equating the slopes of the two regions. This approach, which we refer to as the "hybrid scheme" can be used when the arrival process is modeled as a general Markov modulated arrival process, and in the specific case of the Markov modulated *fluid* source, P_l is expressed by a single exponential as in Equation (3). For example, for an aggregate Markov modulated Fluid source with

¹While the preterm K is different for tail and loss probability, since effective bandwidth approximates K by 1, it does not distinguish between the two.

mean arrival rate λ , stationary probability π_i of being in state *i*, and arrival rate λ_i corresponding to state *i*, the probability of loss is given by:

$$P_l = \frac{1}{\lambda} \sum_{\substack{i \\ \lambda_i > C}} \lambda_i \pi_i \left(1 - \frac{C}{\lambda_i} \right) e^{-\delta B}.$$
(6)

In [14], Elwalid et al. observed that for Markov modulated fluid sources, the loss curve approximation of Equation (3) could be improved by approximating the asymptotic constant K by the loss probability in a bufferless multiplexer as estimated by Chernoff's theorem, and using δ as the same dominant eigenvalue for Markovian sources as in the effective bandwidth result. In particular, denoting R_j as a random variable with the steady-state rate distribution of source j (e.g., R_j 's distribution is given by Equation (1) for on-off sources), K is given by²

$$K = K' \exp\left(-\sup_{s \ge 0} \{sC - \sum_{j} \log Ee^{sR_j}\}\right),\tag{7}$$

where K' is a further refining term given by Equation (55) of [14]. K' is based on Bahadhur Rao asymptotics and we include it in our implementation of this approach.

Consequently, since K can in practice be substantially less than 1 (its approximated value for additive effective bandwidths), algorithms utilizing this term can have improved accuracy as compared to effective bandwidth tests.

2.4 Maximum Variance Based Approaches

We classify the next group of admission control algorithms as Maximum Variance (MV) Approaches. Defining X_t as

$$X_t = \sum_j A_j[s-t,s] - Ct, \tag{8}$$

the tail probability is given by [34]

$$P(Q > B) = P\left(\sup_{t \ge 0} X_t > B\right).$$
(9)

MV approaches are based on the observation that if X_t is Gaussian, one can derive accurate bounds and approximations to the right hand side of Equation (9). As X_t is composed of the aggregate arrivals from a large number of sources, this may be a reasonable assumption in high-speed networks. For Gaussian X_t , the normalized maximum variance of X_t , given by

$$\sigma_B^2 = \max_t \frac{\operatorname{var}\{X_t\}}{(B - E(X_t))^2},\tag{10}$$

plays an important role in evaluating the maximum probability $P(\sup_{t\geq 0} X_t > B)$. For example, the time-instant \hat{t} at which $\frac{\operatorname{Var}\{X_t\}}{(B-E(X_t))^2}$ achieves its maximum value σ_B^2 is the same time-instant at which $P(X_t > B)$ achieves its maximum value. Hence, one approximation used to estimate Equation (9) is

$$P\left(\sup_{t\geq 0} X_t > B\right) \approx \max_t P(X_t > B).$$
(11)

It can be easily seen that the resulting approximation $\max_t P(X_t > B)$ is a lower bound to the tail probability of the buffer occupancy distribution, and is quite easy to compute. Choe and Shroff [16] have shown through an extensive empirical study that Equation (11) is quite accurate when the arrival process can be effectively modeled as a Gaussian process. In [16], the authors have also developed an asymptotic (in terms of B) upper bound based on the normalized maximum variance σ_B^2 , which they refer to as the Maximum Variance Asymptotic upper bound or the MVA upper bound. The authors show that the MVA upper bound in practice behaves like a global upper bound, and together with the lower bound encapsulates the tail probability within a narrow envelope. More recently, the MVA approach has been extended by Kim and Shroff [17] to also estimate P_l by normalizing the MVA upper bound by the exact probability of loss in a bufferless system.

²The supremum can be replaced by *max* when the maximum exists, otherwise it is the least upper bound.

Knightly proposed a related technique using the perspective of stochastic traffic envelopes [18]. A stochastic traffic envelope bounds some statistical properties of $A_j[s, s + t]$ as a function of the interval length t. In particular, traffic is characterized via a *rate-variance envelope* defined by:

$$RV_j(t) \ge \operatorname{var}\left(\frac{A_j[s,s+t]}{t}\right)$$
(12)

which describes a flow's second moment correlation structure. Based on the flows' $RV_j(t)$ characterizations as well as their mean rates, admission control tests are devised whereby the stochastic envelope of the aggregate traffic is approximated with a Gaussian envelope with variance $\sum_j t^2 RV_j(t)$ over intervals of length t. The envelope-based tests then consider the maximal buffer overflow probability in all interval lengths up to the maximal busy period. Consequently, the shape of the loss curve is determined by the properties of the aggregate envelope.

2.5 Refinements to Effective Bandwidths and Large Deviations

Two key shortcomings of the additive effective bandwidth approach are 1) the result is not applicable to traffic sources which exhibit long range dependence and 2) by adding the bandwidth requirements of sources, the effects of economies of scale with a large number of sources are not exploited.

An alternative definition of effective bandwidth is given by [35, 36, 37]

$$E_j(s,t) = \frac{1}{st} \log E e^{sA_j[0,t]}$$
(13)

so that the tail probability of the queue length distribution satisfies

$$\lim_{N \to \infty} \frac{1}{N} \log P(Q > B) = \sup_{t} \inf_{s} \left[st \sum_{j} \rho_{j} E_{j}(s, t) - s(b + ct) \right]$$
(14)

scaling resources to C = Nc, B = Nb, and $N\rho_i$ sources of type j.

This result is based on Large Deviations theory, which is also applied in several other approaches above and has been widely used in providing general results on the asymptotic behavior of $\log P(Q > B)$ [38, 36, 39]. Here, we briefly review related Large Deviations techniques. In [39] for example, Glynn and Whitt show that for a large class of stochastic processes

$$\log P(Q > B) \sim -\delta B. \tag{15}$$

However, for many important types of processes, such as self-similar or other long-range dependent processes [40, 41], the tail probability may not be exponential, and more generally, even (15) may not hold. To address this problem, Duffield and O'Connell exploit the generality of Large Deviation techniques [36] and extended the above result through an elegant scaling technique to obtain

$$\log P(Q > B) \sim -g(B),\tag{16}$$

where g(B) is some increasing function of B, which may not be linear in B. However, the significant generality of this result does come at a cost, namely, poor "resolution", as the similarity relation given by (16) captures only the leading (most rapidly growing) term of $\log P(Q > B)$. For example, if g(B) = B satisfies (16), then $g(B) = B + \sqrt{B}$ also satisfies (16), even though it is a very different function of B. Therefore, in general, approximations for P(Q > B) based on (16) should be used with some caution, since (16) provides relatively weak theoretical support to the asymptotic behavior of these approximations (note that compared to Equation (3), which shows similarity, the large deviation results only show log-similarity).

Recent work has focused on the asymptotic behavior of P(Q > B) when the number of sources, the queue size, and the service rate are all proportionally sent to infinity (e.g. [38]). This limit is quite a different limit from the one in Equation (16). However, such results have generated approximations such as the one in [38] that when applied to Gaussian processes produce the same expression as the MVA upper bound discussed above. This approach also allows for the use of the Bahadhur Rao asymptotics (or Local Central Limit Theorem, also used in Section 2.3) to strengthen the log-asymptotic results considerably (e.g. [42, 43]). In [43], the approximation based on the Bahadhur Rao asymptotics results in the same expression as the MVA lower bound which we consider in this paper. We make the following observations about this class of approaches. First, these effective bandwidths are not "additive" in the same sense as the previous approaches in that the resources required for a particular source depend on the properties of all other sources (the dependencies are through the parameters s and t). Thus, these approaches achieve economies of scale in the number of multiplexed sources and, as we will show in Section 3, are considerably more accurate than the previous additive effective bandwidth techniques. Second, we observe that without further assumptions on the traffic flows, admission control tests in this class can be computationally expensive in their calculation of the supremums in Equation (14). Nevertheless, we show in Section 3 that such approaches can work quite well empirically; moreover, they can address cases of non-Gaussian traffic which the maximum-variance approaches discussed in Section 2.4 cannot.

3 Experimental Evaluation of Admission Control Tests

In this section, we evaluate the accuracy of the aforementioned admission control algorithms by performing a set of simulation and admission control experiments. We consider two types of traffic:

- Actual traces of MPEG-compressed video.
- Markov modulated on-off sources, with on and off times distributed according to standard voice models.

We consider various scenarios with different loads, QoS parameters, etc., and compare the actual admissible regions and QoS values obtained in simulations with those predicted by the admission control tests.

Throughout the experiments, we focus on the following performance metrics. The first is the average utilization of the link, which is the total average rate of all flows divided by the link capacity. For the simulation, this average utilization is also the total number of bits transmitted by the sources in the simulation, divided by the total number of bits that the server can transmit over the duration of the simulation (the link capacity multiplied by the simulation time). Our second performance metric is P(Q > B), the tail of the queue length distribution. For simulations this corresponds to the fraction of time an infinite-buffer queue's occupancy exceeds B. The third performance metric is the empirical fraction of packets that are dropped due to buffer overflow in a *finite*-buffer queue with maximum buffer space B. We denote this measure of loss probability by P_l . In both cases, we consider a range of buffer sizes B which have a corresponding statistically-guaranteed delay bound d = B/C.

3.1 Experimental Evaluation for Video Traces

Here we consider a thirty minute trace of MPEG-compressed video which exhibits statistical properties characteristic of long-range-dependent traffic [18].

3.1.1 Scenario

The video is taken from an action movie, digitized to 384x288 pels and compressed at 24 frames per second using the MPEG 1 compression algorithm with frame pattern *IBBPBBPBB* [44]. For the simulations, we consider each frame to be transmitted at a constant rate over the frame time, $\frac{1}{24}^{th}$ of a second.

For the trace-driven simulations, a simulation cycle runs until all sources transmit their entire trace twice, with the traces wrapped around to the beginning when they reach the end. The first run through the traces is discarded as a transient, and statistics are collected on the second pass through the traces. In a particular scenario, N flows are multiplexed on a 45 Mbps link, with each flow's arrival pattern given by the movie trace, and a start time chosen uniformly over the length of the trace. For the purpose of obtaining small confidence intervals at low loss probabilities, ten thousand such simulation were performed, each with independent start times. We calculate 95% confidence intervals for each probability estimated via simulation using the method of batch mean [45]. However, since the confidence intervals are so small (the max and min of the error bars virtually overlap each other), we do not show them in the figures.

3.1.2 Tail Probability for Multiplexed Video Flows

The experiments reported in Figures 1 and 2 (for the tail and loss probabilities, respectively) are based on the above simulation scenario for a fixed utilization of 84%, which corresponds to 69 video flows on the 45 Mbps link.

Figure 1 depicts the tail probability versus the delay that a packet experiences in queue. In this scenario, even if a multiplexer delays a packet beyond its deadline, the packet is not dropped, but held in the buffer in case its delay could be made up down-stream.

The curve labeled "Simulation" reports the actual fraction of time the buffer exceeds the threshold B or the equivalent delay bound. Notice that this curve drops sharply until buffer sizes of approximately 10 msec, after which it flattens considerably, indicating significant benefits for adding buffer space to a multiplexer, but in this case, only to the extent of a 10 msec delay.



Figure 1: Tail Probability Comparisons for Video Sources

To obtain the upper curve of Figure 1 labeled "Effective BW", we implemented the admission control algorithm Equations (2) and (4). As described in Section 2, the effective bandwidth approximation assumes that the loss (or tail) probability decays exponentially with increasing delay or buffer size, hence the relationship is linear on the figure's semi-log scale. The simulations indicate that the actual loss probabilities for a given buffer size are considerably lower than that predicted by the effective bandwidth scheme; moreover, the measured relationship between loss probability and buffer size is not exponential.

The "Chernoff DE" approach refines the effective bandwidth result by adding a preterm to account for the loss probability in a bufferless multiplexer. We compare the result in this figure to the exact tail probability, since it is usually closer to the tail probability than the corresponding loss curve (e.g., compare this curve to the exact loss curve in Figure 2). Here, the tail probability is approximated by $Ke^{-\delta B}$ with K given by Equation (7), and δ calculated the same as for effective bandwidth. In these experiments, the preterm is K = 0.09 which correspondingly improves the estimate of the tail probability by that factor. However, as shown in the figure, the estimate of P(Q > B) is still conservative by approximately 4 orders of magnitude for buffer sizes above 10 msec. Regardless, the asymptotic slopes of the effective bandwidth and Chernoff Dominant Eigenvalue curves do match the slope of the "Simulation" curve in the region of 10-50 msec, indicating that [8] does provide a good estimate of δ . Unfortunately, this does not necessarily correspond to a good estimate of P(Q > B).

The curve labeled "MVA Upper Bound" provides an asymptotic upper bound to the tail probability as described in [16] without assuming a specific shape of the loss curve. From the figure, we note that this admission control curve follows the measured tail probability quite accurately, including emulating its two-segment shape. Moreover, although this approach is an asymptotic upper bound, empirical results suggest that behaves as a global upper bound, as is the case in Figure 1. Here, we again note that when the large-deviations based expression for the tail probability in [38] is applied to the Gaussian arrival case, the resulting tail probability yields the same curve as the MVA upper bound.

The curve labeled "Lower Bound" has been theoretically investigated in various papers in the context of both Large Deviation techniques and Extreme Value Theory [38, 16, 43]. An extensive study in [16] showed that the lower bound provides an accurate estimate to the tail probability and like the MVA upper bound, closely matches the shape of the tail probability curve. Consequently, the MVA upper and lower bounds envelope the measured tail probability to approximately within an order of magnitude. Finally, we note that the "Rate-Variance" approach for the loss probability (shown in Figure 2), while devised using an entirely different technique with stochastic envelopes, is in fact the same curve as the "Lower Bound" shown here [18].

3.1.3 Loss Probability for Multiplexed Video Flows

Figure 2 depicts the loss probability versus delay for the case in which a packet is dropped at the multiplexer if it violates its delay requirement d, i.e., the actual buffer size of the multiplexer is B = Cd.



Figure 2: Loss Probability Comparisons for Video Sources

The curve labeled "Simulation" reports the actual fraction of packets dropped due to buffer overflow. Notice that this curve is quite similar to the simulated tail curve, except that it is one to two orders of magnitude lower than the corresponding curve shown in Figure 1. The curve labeled "Avg/Peak" refers to the results of our implementation of [7]. For small buffers, the Avg/Peak admission control test over-estimates P_l by only one order of magnitude. However, since this test assumes a bufferless multiplexer, it is increasingly inaccurate for larger buffer sizes.

The "Hybrid" curve refers to the admission control test in [15]. Although the hybrid scheme captures the effect of statistical multiplexing and results in an improvement over the effective bandwidth curve, it too is significantly inaccurate in capturing the exact loss probability. The reason is that the hybrid scheme is based on the "burst region" being of a single exponential type. However, for sources that are correlated at multiple time-scales (such as the MPEG-video example shown here), the loss probability curve does not converge to its asymptotic decay rate quickly (even if there exists an asymptotic decay rate), and hence approximations such as the hybrid scheme perform quite poorly.

The curve labeled "Rate-Variance" (or MVA "Lower Bound") in Figure 2 depicts the results of the admission control test in [18]. This admission control test is able to capture the non-exponential relationship between loss and delay, and although theoretically, the curve is a lower bound to the tail probability, it empirically behaves like an upper bound to the loss probability.

Finally, the curve labeled "MV Approx" is the result of mapping the MVA upper bound for the tail probability to the loss probability in a finite buffer system [17]. This curve follows the simulated tail probability quite closely, capturing the non-exponential nature of the loss curve.

3.1.4 Admissible Region for Multiplexed Video Flows

An admission control test's effectiveness is ultimately determined by its ability to correctly decide whether or not a new traffic flow can be admitted while still satisfying the QoS constraints of all established flows plus the new one. Figure 3 evaluates a number of admission control tests in such a manner.



Figure 3: Admissible Region Comparisons for Video Sources

For a tail probability of 10^{-6} , the figure shows the maximum number of admissible flows, expressed as average utilization, versus delay or buffer size. A point on one of the curves indicates the maximum value of N for the corresponding delay and tail probability. The simulation curve depicts the *measured* admissible region, whereas the other curves depict the admissible regions estimated by the corresponding admission control tests. A desirable property of an admission control algorithm is that its admissible region be as close as possible to, but not greater than, the simulation curve. In other words, the goal is to utilize resources as highly as possible without admitting more flows than can actually be supported, which would result in violations of the promised QoS.

From 1 msec to 50 msec delays, the trace-driven simulation curve of Figure 3 shows the actual achievable average utilization of the multiplexer is in the range of 58% to 85%. Such high utilizations indicate that these MPEG-compressed video flows are well suited to statistical multiplexing despite their burstiness over multiple time-scales. Note also that, as in Figure 3, buffering has a considerable advantage up to approximately 10 to 20 msec; but beyond that, additional buffering does not significantly increase the admissible region.

Of these admission control algorithms, the MVA upper bound (for the tail probability) most closely approximates the measured admissible region, with the MVA loss, lower bound, and rate-variance tests also approximately following the true admissible region and capturing trends such as the relative benefits of adding buffer space. The remaining approaches are significantly more conservative. We investigate the reasons for these experimental observation in Section 4.

3.2 Empirical Evaluation for Voice Sources

In this section, we evaluate the admission control tests for input traffic that is modeled via Markov Modulated on-off processes. We use this model for two reasons: first it provides a baseline for comparison of the admission control tests under a simpler and more widely studied scenario. Second, this model is an accurate and accepted model for voice traffic as it captures the behavior of encoded voice by alternating between "active" (on) and "inactive" (off) states.

3.2.1 Scenario

For our experimental setup, we again consider a 45 Mbps link serving multiplexed voice sources. With encoded voice's alternation between active and inactive states, Markov modulated on-off processes have frequently been used to model voice traffic [46, 47]. A Markov modulated on-off source is one in which traffic is transmitted only in the on-state, and the source spends an exponentially distributed duration of time in the on and off states. In theory, one could solve a series of equations (balance equations) to calculate the exact loss or tail probability for a fluid queue serving on-off sources. However, in this case, since well over a thousand voice sources can be multiplexed on a 45 Mbps link, such an exact analytical solution becomes computationally infeasible. Hence, we again use simulations to evaluate the various admission control algorithms.

For these simulations, we assume a 1 msec slot size and use a discrete-time on-off Markov Modulated Fluid process as a voice source model. For each source, when in the on-state traffic is generated with a fluid rate of 0.85 cells/second (which corresponds to 32Kbps for an ATM size cell). Further, for each source, let p_{ij} correspond to the transition probability from state *i* to state *j* (for i = 0, 1 and j = 0, 1), where state 0 corresponds to the off-state, and state 1 corresponds to the on-state. Then, $p_{00} = 0.9983$, $p_{01} = 0.00167$, $p_{10} = 0.0025$, $p_{11} = 0.9975$. To obtain reliable results at very low loss (or tail) probabilities we use the *importance sampling* simulation technique described in [28].

3.2.2 Tail Probability for Voice Sources

The experiments reported in Figures 4 and 5 (for the loss and tail probabilities, respectively) are based on the above simulation scenario with a utilization of 93%, which corresponds to 2900 voice flows on the 45 Mbps link.

Figure 4 depicts the tail probability versus delay that a packet experiences in the queue. As in the case for MPEG video, in this scenario, even if a packet's deadline is violated at a queue, the packet is not dropped, but held in case its delay could be made up down-stream.

Once again, note that the additive effective bandwidth approach results in a curve that is quite conservative, and results in almost a 4 orders of magnitude overestimate of the tail probability. However, in this case, the Chernoff Dominated Eigenvalue approach of [14] performs better than in the case of multiplexed video. The reason for this is that the prefactor term used in [14] helps capture the statistical multiplexing gain due to the aggregation of the sources. Since multiplexed on-off sources do not exhibit strong multi-time scale correlation, the single exponential approximation does manage to provide a reasonable match with simulations (even though for larger buffer size the mismatch is almost two orders of magnitude). The MVA upper bound and the lower bound both accurately track the tail probability and encapsulate it within a relatively narrow envelope.



Figure 4: Tail Probability Comparisons for On-Off (Voice) Sources

3.2.3 Loss Probability for Voice Sources

Figure 5 depicts the loss probability versus delay for the case in which a packet is dropped at the multiplexer if it violates its delay requirement.

The simulation curve again reports the actual fraction of packets that exceed the buffer level (or equivalently the delay requirement). For small buffers, the Avg/Peak admission control test is more accurate than the effective bandwidth test, but again becomes increasingly inaccurate for larger buffer sizes due to the assumption of a bufferless multiplexer.

The "Hybrid" scheme [15] accurately captures the effect of statistical multiplexing, and as can be seen in Figure 5, accurately captures the loss probability for small buffer values. However, similar to the case of the Chernoff Dominant Eigenvalue approach, for large values of delay, the scheme can overestimate the loss probability by up to two orders of



Figure 5: Loss Probability Comparisons for On-Off (Voice) Sources

magnitude. The "Rate-Variance" (or MVA "Lower Bound") approach performs worse than the hybrid scheme until larger buffer sizes, and the "MV Approx" curve [17] most closely follows the measured loss curve.

3.2.4 Admissible Region



Figure 6: Admissible Region Comparisons for On-Off (Voice) Sources

In Figure 6 we compare the simulated admissible region with those of the admission control algorithms. Following the approach taken earlier, for a tail probability of 10^{-6} , the figure shows the maximum number of admissible traffic flows, expressed as average utilization, versus delay or buffer size. The simulation curve of Figure 6 shows the actual achievable average utilization of the multiplexer is in the range of 91% to 94% or 3198 to 3303 multiplexed flows. These high utilizations are again due to the fact that voice traffic is well suited to taking advantage of a statistical multiplexed system.

Of these admission control algorithms, the Rate Variance approach (or MVA Lower Bound) most closely approximates the measured admissible region, but being a lower bound, slightly exceeds the admissible curve. The MVA upper bound

follows the admissible region curve quite well, while being somewhat conservative (a useful feature for admission control). In this case, the Chernoff Dominant Eigenvalue approach and Ave/Peak test also work reasonably well (the latter being increasingly worse for larger allowable delays), while the additive effective bandwidth approach is again quite conservative.

4 Admission Control Tests: Approximations and Accuracy

4.1 The Rationale of Gaussian Modeling

The experiments of Section 3 have shown that modeling the aggregate arrival process as a general Gaussian process results in good estimates of the tail probability even when the number of sources multiplexed is moderate (as in the case of the video sources). As discussed previously, the Gaussian characterization is motivated by the Central Limit Theorem, since a link in a high-speed network is expected to carry many traffic sources. One advantage of a Gaussian characterization versus other types of models is that it requires less detailed knowledge of the source than for example Markov arrival models. However, one could then ask the question, why not appeal to a Poisson limit theorem and characterize the aggregate traffic to a multiplexer as a Poisson Process (after all the Poisson Process can be characterized simply by its mean). The reason is quite simple: the Poisson Limit theorem involves a very different type of scaling, and the Poisson traffic characterization destroys the temporal correlation structure of the traffic, in fact making it memoryless (independent and stationary increments!). Since real traffic is highly correlated, a Poisson characterization results in grossly incorrect loss (or tail) probability calculation, and hence a wrong admissible region. The Gaussian characterization, on the other hand, is very useful since it allows for different correlation structures (any function can be a valid autocovariance function), and hence captures the temporal correlation of the traffic. As an illustrative example, using the techniques of [48], one can compute the loss probability for fractional Brownian motion, a self-similar process, as a trivial special case, as it merely represents a particular autocovariance function.

4.2 Impact of Buffering

The experiments of Section 3 evaluate the impact of buffer-size scaling on both the multiplexer's performance as well as the effectiveness of the different admission control algorithms. The trace-driven simulation experiments indicate that even for highly correlated traffic some buffering is of substantial benefit. For example, our simulations show that with 66 multiplexed MPEG flows, 30 msec or approximately 170 kBytes worth of buffering decreases the loss probability from .003 to $7 \cdot 10^{-7}$. Further, considering the admissible region and a loss probability of 10^{-6} , 30 msec of buffering increases the admissible region from 49 to 66 flows, for a 35% improvement. As noted in Section 3, the incremental advantages of an increased buffer size do not extend indefinitely, but rather decay quickly once the multiplexer has 10 to 20 msec of buffering. In the case of on-off sources, buffering is of lesser benefit in that it does not result in as significant an increase in the admissible region. However, in real systems one expects a mix of both multi-time scale correlated traffic such as voice, so that the resulting aggregate traffic will indeed exhibit multi-time scale properties. Hence, the conclusions about buffers drawn from the experiments with video traces are more relevant in realistic network design.

Thus, for the video sources with the importance of buffering in the actual system, admission control tests that take into account buffer size scaling are able to significantly out-perform those that do not. Indeed, the Avg/Peak admission control test of [7] is one of the more conservative tests partially because of its assumption of a bufferless multiplexer.

We note however, that the aforementioned 35% increase in the admissible region of Figure 3, or the 4 orders-ofmagnitude decrease in the loss probability, comes at a cost: the costs of the memory itself; buffer management costs; and potential increased complexity in the admission control tests, as tests incorporating network buffers must also consider the traffic's autocorrelation structure.

4.3 Economies of Scale in the Number of Flows

As the number of multiplexed sources N increases, the amount of resources (bandwidth and buffer space) that must be reserved *per source* should decrease as an effect of statistical multiplexing and a simple consequence of the law of large numbers. In other words, we expect to have economies of scale in the number of multiplexed sources. While most admission control tests we considered exploit such economies of scale, additive effective bandwidth tests do not, since such tests determine a flow's resource demands using only the stochastic properties of the source itself (e.g., its index of dispersion), independent of the properties of other sources or the total number of sources being multiplexed. Indeed, independently

summarizing the resource requirements of heterogeneous and bursty traffic sources by per-flow bandwidths was exactly the goal of the original work on additive effective bandwidths. However, as is evident from Figure 3, the approach's lack of N scaling significantly limits the achievable utilization.

4.4 Loss Curve

The relationship between the packet loss probability and the buffer size as in Figure 3 is often referred to as the loss curve. While the ultimate goal of an admission control test is to correctly determine the admissible region, many admission control tests have been designed with an intermediary focus on the shape of the loss curve. For example, [14] is motivated by the dominant eigenvalue of Markovian sources to approximate the loss curve with an exponential relationship $P_l \approx K e^{-\delta B}$. Effective bandwidth schemes also assume an exponential relationship but with $K \approx 1$.

Our simulation results of Figure 3 depict a loss curve that is significantly different from exponential. While long range dependence is a plausible explanation for this [38], it could also be that the multiple-time-scale correlation of the sources results in this very slow convergence of the loss (or tail) probability to its asymptotic slope.

We note that the maximum variance based admission control tests of Section 2.4 are able to track this non-exponential loss curve quite well. These tests do not assume that traffic flows are long range dependent, but rather use a general second moment traffic description to obtain the required loss (or tail) curves.

In [14], trace drive simulations were also performed and the reported loss curves are nearly exponential. Consequently, the Chernoff Dominant Eigenvalue test of [14] was quite accurate for those experiments. While we found corroborating results for *voice* sources, for video sources we found that the measured tail or loss curve is far from exponential so that the Chernoff Dominant Eigenvalue test is considerably less accurate. This may have been due to a combination of the fact that (1) [14] used a videoconference trace which likely does not exhibit multi-time-scale rate variation; and (2) [14] used JPEG-rather than MPEG-compressed video, with the latter having substantially more rate variation on small time scales as well.

Here we note that for sources that are correlated over small time scales (e.g., the on-off voice sources), any admission control test that accurately estimates the statistical multiplexing gain via the prefactor K in front of the exponential in Equation (3), will capture the loss (or tail) probability quite well. However, techniques such as the additive effective bandwidth that are unable to capture this statistical multiplexing gain, or techniques such as the Ave/Peak combinatorics that do not account for non-zero buffers, will still tend to be rather conservative.

4.5 Important Traffic Parameters

In addition to assumptions about the shape of the loss curve and network buffer sizes, an admission control test must characterize traffic flows according to a parameterized traffic model.

The on-off traffic model used in the admission control test of [7] is the simplest of the models we considered here (indeed, peak and average rate are likely the minimum amount of information needed to provide a statistical service). While this model is simple and closely related to standard traffic models (which specify peak rate, average rate, and burst length), it is also quite closely tied to the assumption of a bufferless multiplexer, which as described above, has a considerable utilization penalty for an admission control test. Indeed, to take into account the effects of buffering, more information is needed about the traffic flows such as their autocorrelation structure, their maximum rates over various interval lengths [49], or at least a burst length parameter.

While many admission control tests can work well with on-off sources, when these same admission control tests are applied to the compressed video sources we have considered here, the tests exhibit considerable inaccuracies. For traffic flows that exhibit multiple time scale rate variation, we argue that refined traffic models (beyond peak and average rate) are needed to extract the full statistical multiplexing gain. For example, the proposed traffic model of [49] characterizes a source by a family of rate-interval pairs where the rate is a bounding rate over the corresponding interval length. Such parameters can also be used to bound or approximate stochastic parameters such as the rate-variance envelope considered here [24, 50]. A second possibility is to have users directly convey their second moment characteristics to the network, which our experimental results indicate can accurately estimate the admissible region. Unfortunately, the downside to incorporating more sophisticated traffic models is two fold: first, additional traffic parameters are needed beyond the standard three parameter models, which also means that policing requires at least multi-level leaky buckets rather than a single leaky bucket (see [49]). Second, the more detailed the traffic parameter, the greater the burden on network clients to accurately characterize their traffic in advance.

It therefore appears that if a refined traffic model is not used, statistical services would yield such low resource utilization for bursty traffic flows that either renegotiated services [51, 5] or measurement based services [19, 20, 21, 22] must be used instead. While such services have their own merits as discussed in the respective works, they unfortunately cannot provide statistical QoS *guarantees* per se. Moreover, a renegotiated service requires increased signaling overhead and a measurement based service must successfully make accurate predictions of future resource requirements using past measurements of aggregate multiple time scale sources, which, as we have seen here, is a difficult problem even when future arrival statistics *are* known.

Lastly, we note that admission control tests differ in their computational complexity or the number of instructions that must be executed upon the arrival of a new admission request. While exploration of this issue is beyond the scope of this current work, we do note that all of the schemes we have considered were designed with implementation considerations, with [7] giving this issue the most attention.

5 Conclusions

From the results of our trace-driven simulations and admission control experiments with a diverse set of admission control algorithms, we make the following observations. (1) Assuming a bufferless multiplexer introduces a substantial utilization penalty if the actual multiplexer does contain buffer space. (2) Economies of scale in the number of multiplexed flows is a crucial component to achieving a high degree of accuracy. (3) Experimentally observed loss curves (loss probability vs. buffer size) for compressed video sources are quite different than the commonly assumed exponential relationship. If indeed the curves do asymptotically (with buffer size) become exponential, the convergence rate is usually quite slow, which renders exponential types of approximations fairly inaccurate over any meaningful buffer size or loss probability. (4) Refinements of current standard traffic models are required in order to obtain a reasonable statistical multiplexing gain and a statistical QoS guarantee. (5) Admission control tests that work demonstrably well with exponential on-off sources can suffer from considerable inaccuracies when applied to multiple time scale sources such as compressed VBR video.

We found that a number of admission control tests from the literature perform quite well experimentally for both on-off sources and compressed video sources, including algorithms by the authors [16, 18] and others [38, 42, 43].

6 Acknowledgements

The authors would like to give many thanks to Jinwoo Choe and Han S. Kim for running the simulations reported in this paper, and for preparing the figures for the paper. The authors would also like to thank the anonymous reviewers for carefully reading the paper, and for their helpful comments.

References

- E. Knightly. On the accuracy of admission control tests. In *Proceedings of IEEE ICNP* '97, pages 125–133, Atlanta, GA, October 1997.
- [2] D. Wrege, E. Knightly, H. Zhang, and J. Liebeherr. Deterministic delay bounds for VBR video in packet-switching networks: Fundamental limits and practical tradeoffs. *IEEE/ACM Transactions on Networking*, 4(3):352–362, June 1996.
- [3] M. Garret and W. Willinger. Analysis, modeling and generation of self-similar VBR video traffic. In *Proceedings of ACM SIGCOMM '94*, pages 269–280, London, UK, August 1994.
- [4] A. Lazar, G. Pacifici, and D. Pendarakis. Modeling video sources for real time scheduling. ACM Multimedia Systems Journal, 1(6):253–266, April 1994.
- [5] H. Zhang and E. Knightly. RED-VBR: A renegotiation-based approach to support delay-sensitive VBR video. ACM Multimedia Systems Journal, 5(3):164–176, May 1997.
- [6] D. Ferrari and D. Verma. A scheme for real-time channel establishment in wide-area networks. *IEEE Journal on Selected Areas in Communications*, 8(3):368–379, April 1990.

- [7] T. Lee, K. Lai, and S. Duann. Design of a real-time call admission controller for ATM networks. *IEEE/ACM Trans*actions on Networking, 4(5):758–765, October 1996.
- [8] C. Courcoubetis and R. Weber. Effective bandwidths for stationary sources. *Probability in Engineering and Informa*tional Sciences, 9(2):285–294, 1995.
- [9] A. Elwalid and D. Mitra. Effective bandwidth of general Markovian traffic sources and admission control of high speed networks. *IEEE/ACM Transactions on Networking*, 1(3):329–43, June 1993.
- [10] R. Guérin, H. Ahmadi, and M. Naghshineh. Equivalent capacity and its application to bandwidth allocation in highspeed networks. *IEEE Journal on Selected Areas in Communications*, 9(7):968–981, September 1991.
- [11] G. Kesidis, J. Walrand, and C. Chang. Effective bandwidths for multiclass Markov fluids and other ATM sources. *IEEE/ACM Transactions on Networking*, 1(4):424–428, August 1993.
- [12] Andrea Baiocchi, Nicola Melazzi, Marco Listani, Aldo Roveri, and Roberto Winkler. Loss performance analysis of an atm multiplexer loaded with high-speed on-off sources. *IEEE Journal On Selected Areas In Communications*, 9(3):388–393, April 1991.
- [13] G. Choudhury, D. Lucantoni, and W. Whitt. Squeezing the most out of ATM. *IEEE Transactions on Communications*, 44(2):203–217, February 1996.
- [14] A. Elwalid, D. Heyman, T. Lakshman, D. Mitra, and A. Weiss. Fundamental bounds and approximations for ATM multiplexers with applications to video teleconferencing. *IEEE Journal on Selected Areas in Communications*, 13(6):1004–1016, August 1995.
- [15] N. Shroff and Mischa Schwartz. Improved loss calculations at an atm multiplexer. IEEE/ACM Transactions on Networking, 6(4):411–422, August 1998.
- [16] J. Choe and N. Shroff. A central limit theorem based approach to analyze queue behavior in ATM networks. *IEEE/ACM Transactions on Networking*, 6(5):659–671, October 1998.
- [17] H. Kim and N. Shroff. Loss probability calculations in a finite buffer queueing system. Technical Report, Purdue University, West Lafayette, IN 47907-1285.
- [18] E. Knightly. Second moment resource allocation in multi-service networks. In *Proceedings of ACM SIGMETRICS* '97, pages 181–191, Seattle, WA, June 1997.
- [19] R. Gibbens, F. Kelly, and P. Key. A decision-theoretic approach to call admission control in ATM networks. *IEEE Journal on Selected Areas in Communications*, 13(6):1101–1114, August 1995.
- [20] S. Jamin, P. Danzig, S. Shenker, and L. Zhang. A measurement-based admission control algorithm for integrated services packet networks. *IEEE/ACM Transactions on Networking*, 5(1):56–70, February 1997.
- [21] J. Qiu and E. Knightly. QoS control via robust envelope-based MBAC. In *IEEE/IFIP IWQoS '98*, Napa, CA, May 1998.
- [22] D. Tse and M. Grossglauser. Measurement-based call admission control: Analysis and simulation. In Proceedings of IEEE INFOCOM '97, Kobe, Japan, April 1997.
- [23] A. Elwalid, D. Mitra, and R. Wentworth. A new approach for allocating buffers and bandwidth to heterogeneous, regulated traffic in an ATM node. *IEEE Journal on Selected Areas in Communications*, 13(6):1115–1127, August 1995.
- [24] E. Knightly. H-BIND: A new approach to providing statistical performance guarantees to VBR traffic. In *Proceedings* of IEEE INFOCOM '96, pages 1091–1099, San Francisco, CA, March 1996.
- [25] S. Rajagopal, M. Reisslein, and K. Ross. Packet multiplexers with adversarial regulated traffic. In *Proceedings of IEEE INFOCOM* '98, San Francisco, CA, March 1998.

- [26] M. Krunz and S. Tripathi. Impact of video scheduling on bandwidth allocation for multiplexed MPEG streams. *Multimedia Systems Journal*, 5(6):347–357, 1997.
- [27] J. McManus and K. Ross. Video-on-demand over ATM: constant-rate transmission and transport. *IEEE Journal on Selected Areas in Communications*, 14(6):1087–1098, August 1996.
- [28] C. Chang. Stability, queue length, and delay of deterministic and stochastic queueing networks. *IEEE Transactions on Automatic Control*, 39(5):913–931, May 1994.
- [29] D. Anick, D. Mitra, and M. Sondhi. Stochastic theory of a data-handling system with multiple sources. *Bell System Technical Journal*, 61:1871–1894, 1982.
- [30] N. Shroff and M. Schwartz. Video modeling within networks using deterministic smoothing at the source. In *Proceedings of IEEE INFOCOM* '94, pages 342–349, Toronto, Ontario, June 1994.
- [31] Ness Shroff. *Traffic Modeling and Analysis in High Speed ATM Networks*. PhD thesis, Graduate School of Arts and Sciences, Columbia University, 1995.
- [32] P. Skelly, M. Schwartz, and S. Dixit. A histogram-based model for video traffic behavior in an ATM multiplexer. *IEEE/ACM Transactions on Networking*, 1(4):446–459, August 1993.
- [33] Ness Shroff and Mischa Schwartz. Modeling vbr video over networks end-to-end using deterministic smoothing at the source. International Journal of Communications Systems, Special Issue on Traffic Management in ATM Networks, 7:337–348, December 1994.
- [34] R. Loynes. The Stability of a Queue with Non-independent Inter-arrival and Service Times. Proc. Cambridge Philos. Soc., 58:497–520, 1962.
- [35] C. Courcoubetis, V. Siris, and G. Stamoulis. Application and evaluation of large deviation techniques for traffic engineering in broadband networks. In *Proceedings of ACM SIGMETRICS* '98, Madison, WI, June 1998.
- [36] N. G. Duffield and Neil O'Connell. Large deviations and overflow probabilities for the general single server queue, with application. *Proc. Cambridge Philos. Soc.*, 118:363–374, 1995.
- [37] F. Kelly. Notes on effective bandwidths. In Stochastic Networks: Theory and Applications. Oxford University Press, 1996.
- [38] D. Botvich and N. Duffield. Large deviations, the shape of the loss curve, and economies of scale in large multiplexers. *Queueing Systems*, 20:293–320, 1995.
- [39] P. Glynn and W. Whitt. Logarithmic asymptotics for steady-state tail probabilities in a single-server queue. *Journal of Applied Probability*, pages 131–155, 1994.
- [40] J. Beran, R. Sherman, M. Taqqu, and W. Willinger. Long-range dependence in variable-bit-rate video traffic. *IEEE Transactions on Communications*, 43(2–4):1566–1579, Feb.–April 1995.
- [41] W. Leland, M. Taqqu, W. Willinger, and D. Wilson. On the Self-Similar Nature of Ethernet Traffic (Extended Version). *IEEE/ACM Transactions on Networking*, 2(1):1–15, Feb. 1994.
- [42] Nikolay Likhanov and Ravi R. Mazumdar. Cell-loss asymptotics in buffers fed with a large number of independent stationary sources. In *Proceedings of IEEE INFOCOM*, 1998.
- [43] M. Montgomery and G. de Veciana. On the Relevance of Time Scales in Performance Oriented Traffic Characterization. In *Proceedings of IEEE INFOCOM*, pages 513–520, 1996.
- [44] O. Rose. Statistical properties of MPEG video traffic and their impact on traffic modeling in ATM systems. In Proceedings of IEEE Conference on Local Computer Networks, pages 397–406, Minneapolis, MN, October 1995.
- [45] P. Bratley, B. Fox, and L. Schrage. A Guide to Simulation. Springer-Verlag, New York, second edition, 1987.

- [46] J. Daigle and J. Langford. Models for Analysis of Packet Voice Communication Systems. *IEEE Journal on Selected Areas in Communications*, 4:847–855, Sep. 1986.
- [47] K. Sriram and W. Whitt. Characterizing Superposition Arrival Processes in Packet Multiplexer for Voice and Data. *IEEE Journal on Selected Areas in Communications*, 4:833–846, Sep. 1986.
- [48] J. Choe and N. Shroff. Queueing analysis of high-speed multiplexers including long-range dependent arrival processes. In *Proceedings of IEEE INFOCOM '99*, New York, NY, March 1999.
- [49] E. Knightly and H. Zhang. D-BIND: An accurate traffic model for providing QoS guarantees to VBR traffic. *IEEE/ACM Transactions on Networking*, 5(2):219–231, April 1997.
- [50] E. Knightly. Enforceable quality of service guarantees for bursty traffic streams. In *Proceedings of IEEE INFOCOM* '98, San Francisco, CA, March 1998.
- [51] M. Grossglauser, S. Keshav, and D. Tse. RCBR: A simple and efficient service for multiple time-scale traffic. *IEEE/ACM Transactions on Networking*, 5(6):741–755, December 1997.